

Exergy analysis and process design

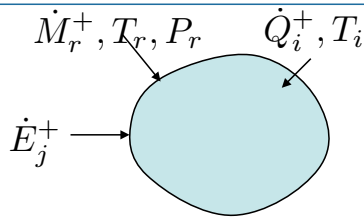
De l'utilisation de l'exergie pour optimiser le design des procédés

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Content

- What is exergy ?
- Exergy efficiency of a process
- Analysing process unit operations & interconnectivity
- Process integration & exergy
- Process design & exergy
- Conclusions

Open system : without accumulation : Energy and entropy balances



First principle: energy balance

Nothing is lost - nothing is created, everything is transformed

$$\sum_j \dot{E}_j^+ + \sum_i \dot{Q}_i^+ + \sum_r \dot{M}_r^+ h_r(T_r, P_r, X_r) = 0$$

Second principle: entropy balance

The entropy of an isolated system tends to increase

$$dS = \sum_i \frac{\dot{Q}_i^+}{T_i} + \sum_r \dot{M}_r^+ s_r(T_r, P_r, X_r) \geq 0$$

Notion of exergy

1st principle: energy balance

$$\sum_j \dot{E}_j^+ + \sum_i \dot{Q}_i^+ + \sum_r \dot{M}_r^+ h_r(T_r, P_r, X_r) + \dot{Q}_a^+ = 0 \quad (1)$$

2nd principle: entropy balance

$$dS = \sum_i \frac{\dot{Q}_i^+}{T_i} + \sum_r \dot{M}_r^+ s_r(T_r, P_r, X_r) + \frac{\dot{Q}_a^+}{T_a} \geq 0$$

$$\Rightarrow T_a dS = \sum_i \frac{T_a \dot{Q}_i^+}{T_i} + \sum_r \dot{M}_r^+ T_a s_r(T_r, P_r, X_r) + \dot{Q}_a^+ \geq 0 \quad (2)$$

$$(1) - (2) \quad \sum_j \dot{E}_j^+ + \sum_i \dot{Q}_i^+ \left(1 - \frac{T_a}{T_i}\right) + \sum_r \dot{M}_r^+ (h_r - T_a s_r) \leq 0$$

then
$$\sum_j \dot{E}_j^- \leq \sum_i \dot{Q}_i^+ \left(1 - \frac{T_a}{T_i}\right) + \sum_r \dot{M}_r^+ (h_r - T_a s_r)$$

therefore
$$E_{max}^- = \sum_i \dot{Q}_i^+ \left(1 - \frac{T_a}{T_i}\right) + \sum_r \dot{M}_r^+ (h_r - T_a s_r) \rightarrow \text{Exergy} = \text{max work}$$

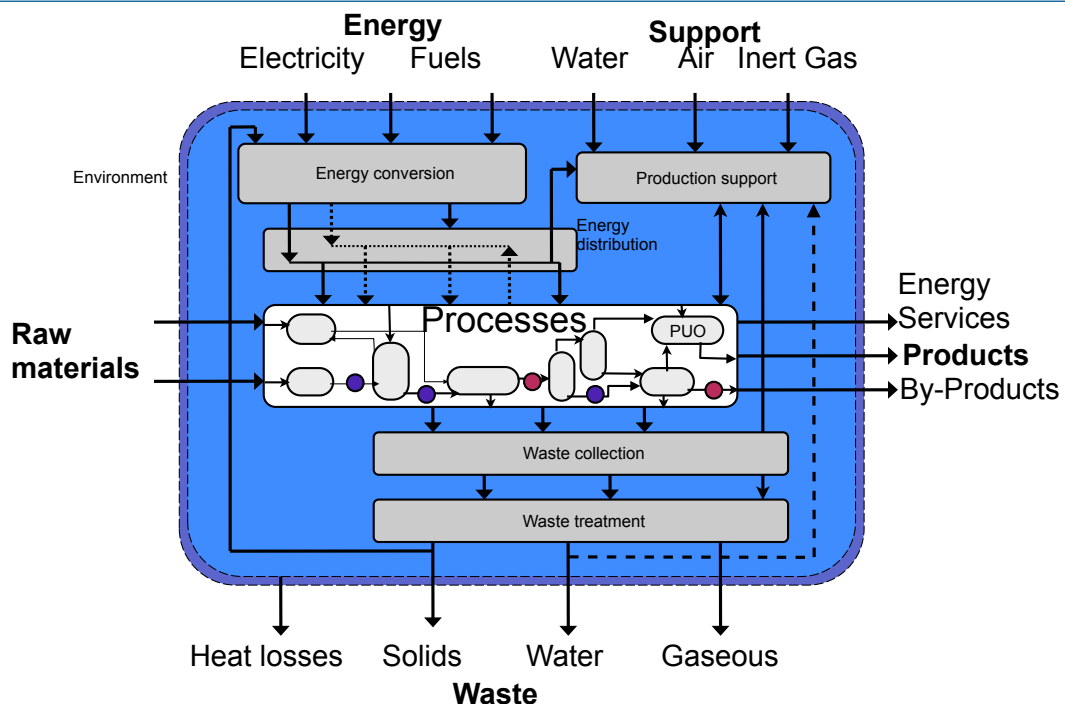
$$\dot{L} = \dot{E}_{max}^- - \sum_j \dot{E}_j^- \geq 0 \rightarrow \text{Exergy loss} \Rightarrow \text{wrt max work}$$

exergy is sometime name availability (of work), exergy loss is the loss of the capacity to produce work, the energy is not lost.

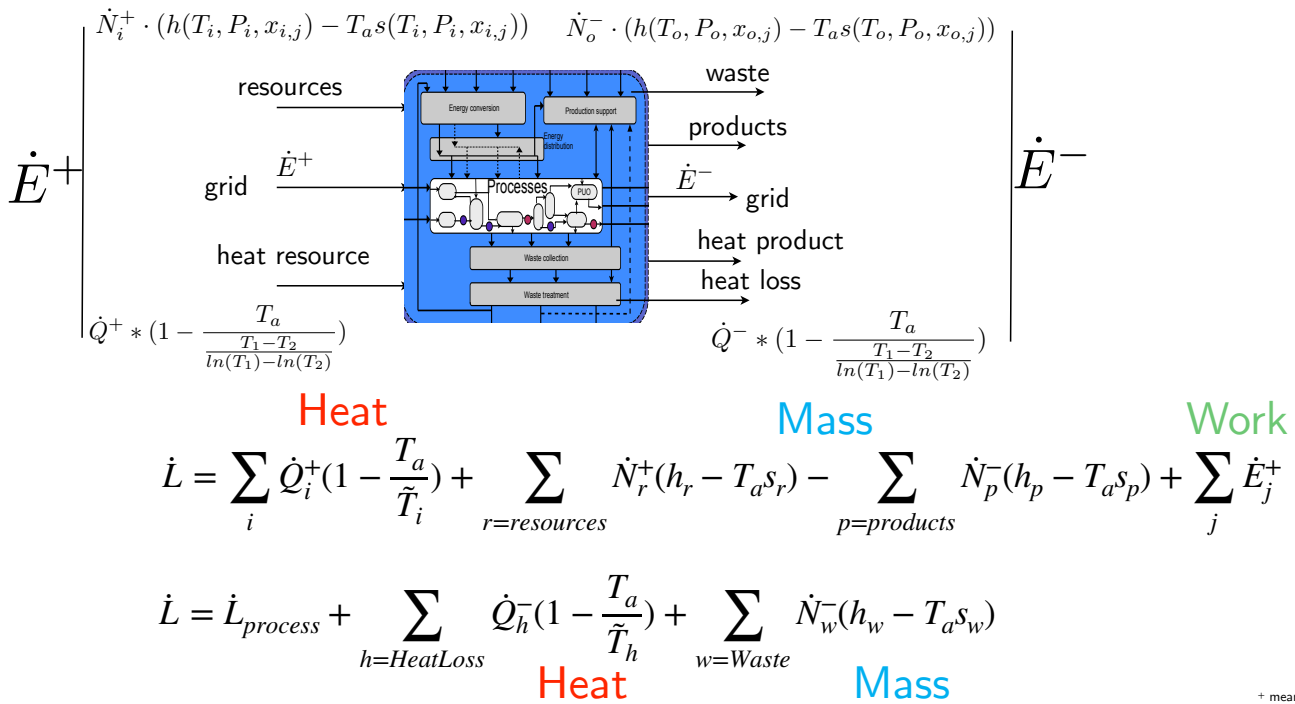
Definition of exergy

The exergy is the amount of **work** that can be produced by converting any thermodynamic states by using **reversible** transformations that **exchange** only with the **ambient conditions** (T_a , X_i , P)

Production process

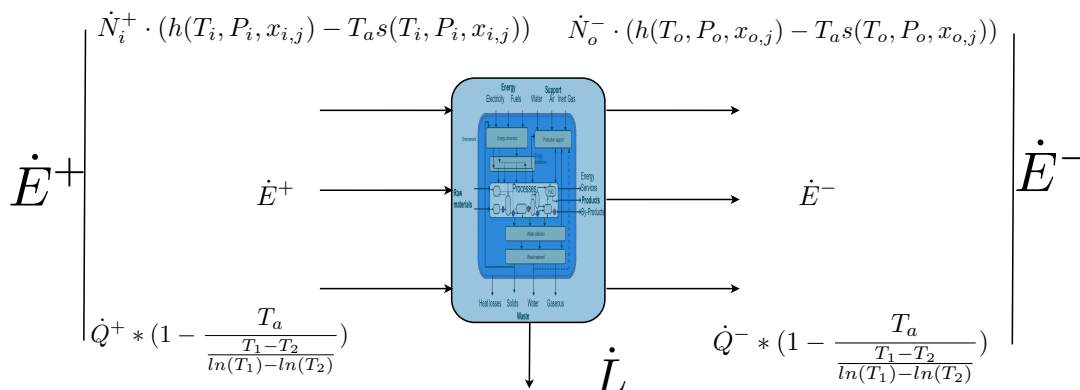


exergy balance of a process



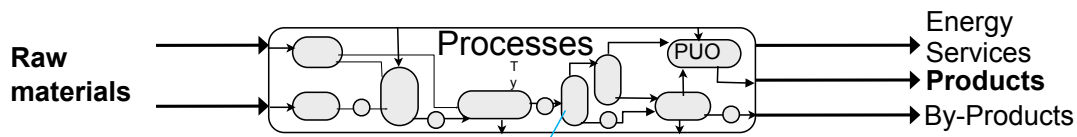
Exergetic efficiency of a process

$$\eta = \frac{\dot{E}^- (\text{delivered})}{\dot{E}^+ (\text{consumed})} = \frac{\dot{E}^+ - \dot{L}}{\dot{E}^+} = 1 - \frac{\dot{L}}{\dot{E}^+}$$

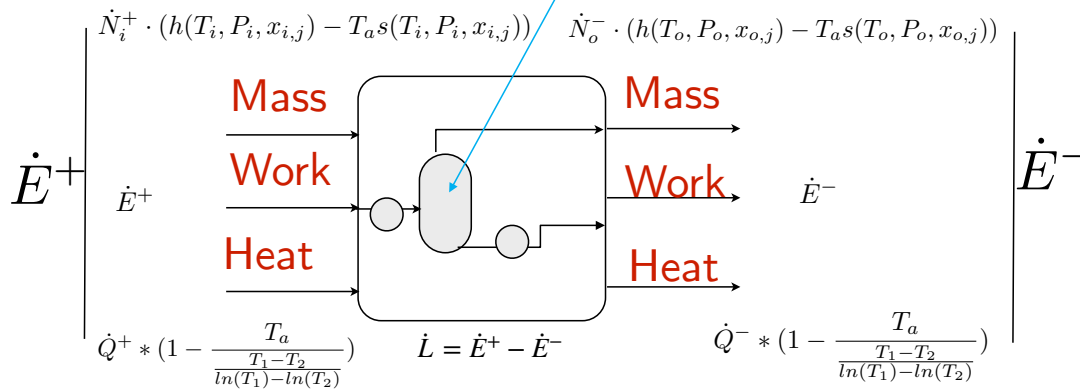


Losses = Exergy in - Exergy out (i.e. used)

In a process, process units exchange mass, heat and work



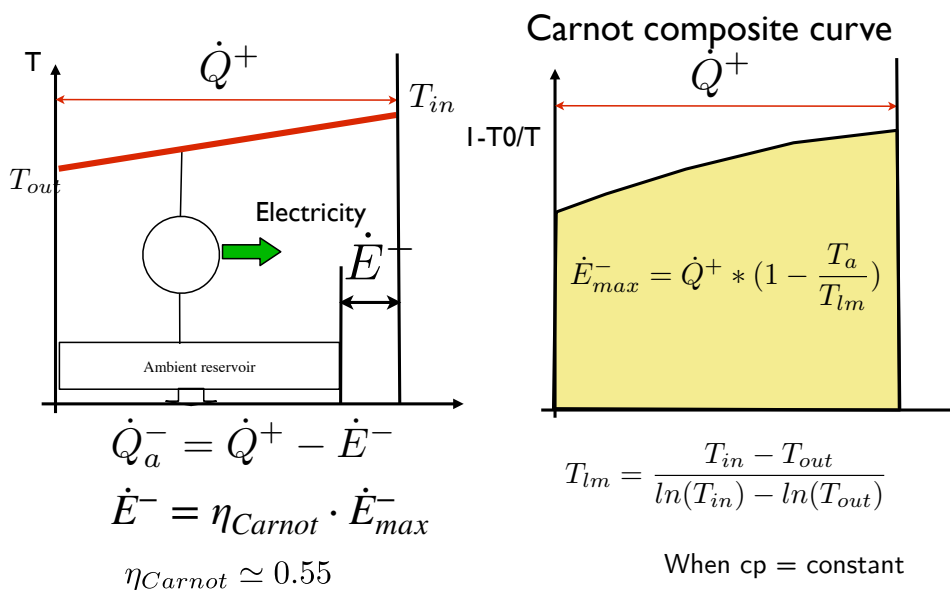
New system boundaries !



Process units exchanges have an exergetic value
Exchanges take place inside the system

The exergy value of a hot stream (heat delivery)

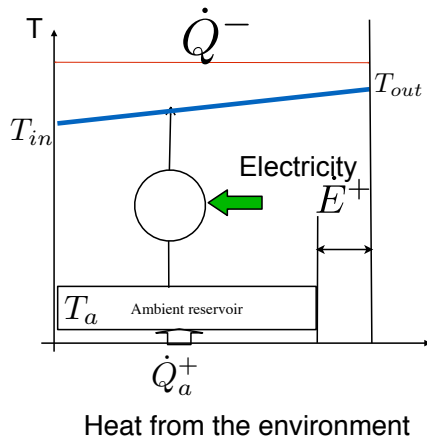
Above the ambience, a hot stream delivers exergy and balances with the environment



The exergy value of a cold stream : heat consumption

above the ambience : A cold stream requires exergy and balances with the environment

$$\dot{Q}^- = \dot{Q}_a^+ + \dot{E}^+$$



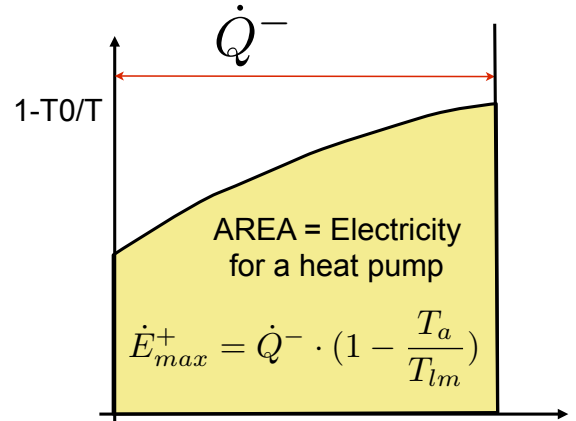
$$\dot{E}_{min}^+ = \dot{Q}^- \cdot \left(1 - \frac{T_a}{T_{lm}}\right)$$

$$T_{lm} = \frac{T_{in} - T_{out}}{\ln(T_{in}) - \ln(T_{out})}$$

$$\dot{E}^+ = \frac{\dot{E}_{min}^+}{\eta_{Carnot}}$$

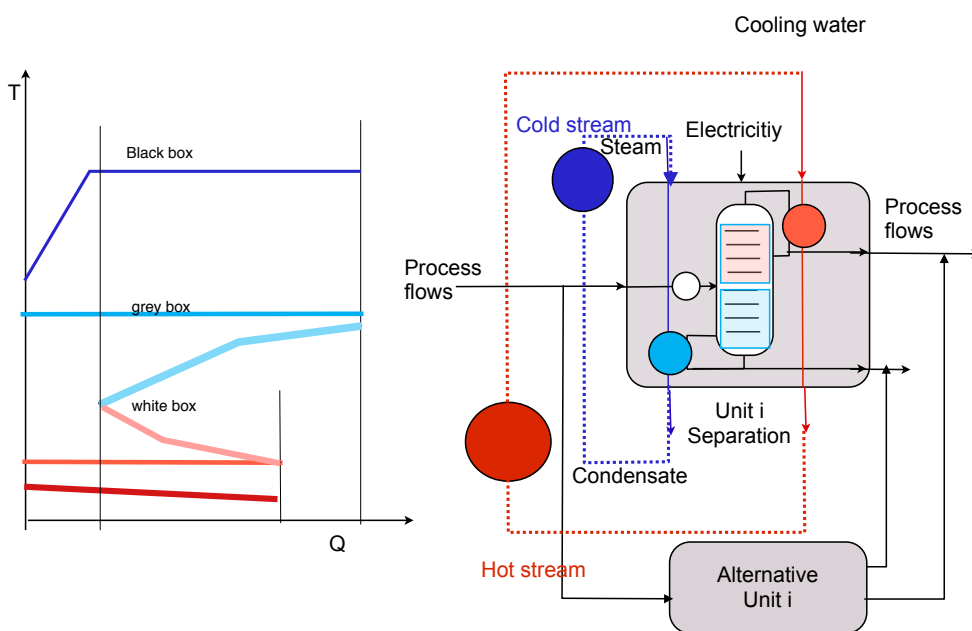
$$\eta_{Carnot} \approx 0.55$$

Carnot composite curve

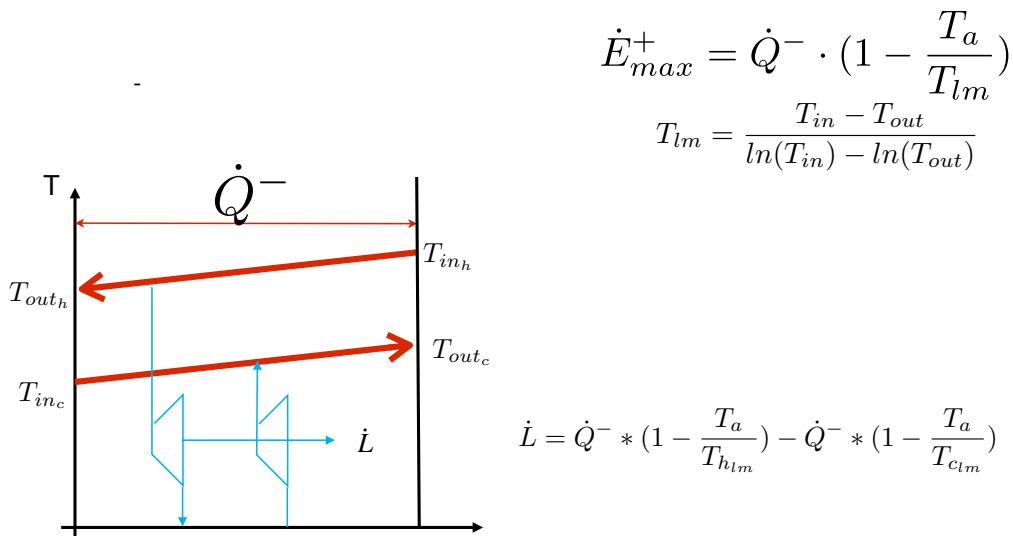


$$T_{lm} = \frac{T_{in} - T_{out}}{\ln(T_{in}) - \ln(T_{out})}$$

Defining Unit Operation heat exchange interfaces



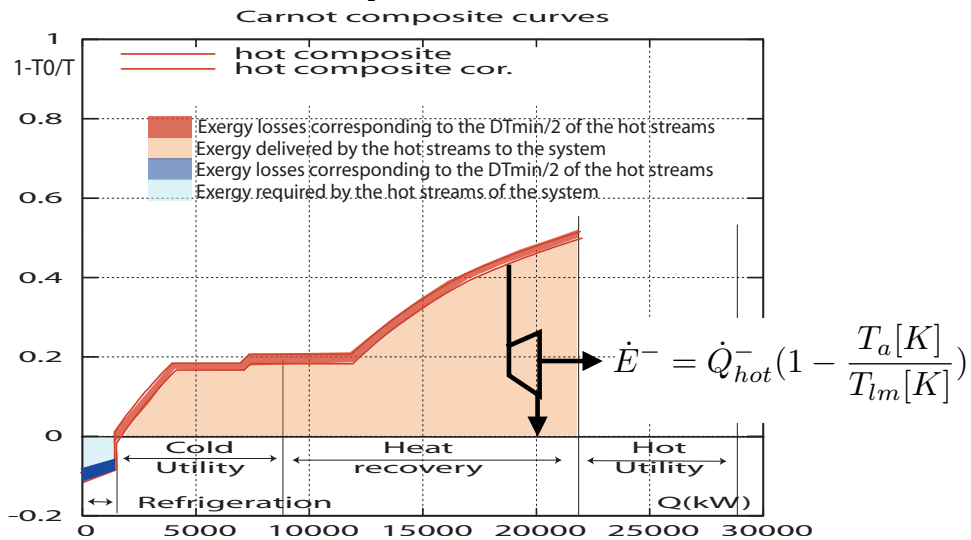
Heat recovery and exergy



The exergy lost in the heat exchanger is the amount of work that can not be produced any more (lost) when the heat exchange is realised. It corresponds to the power that could be produced if one installs an infinite number of perfect Rankine cycles between the hot and the cold streams of the heat exchanger

Carnot composite curves of a process

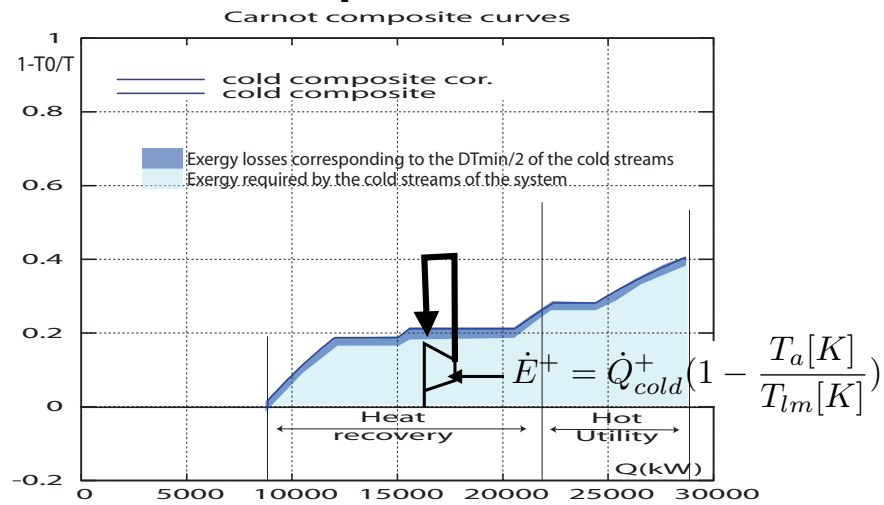
Hot composite curves



This is the exergy made available by all the hot streams in the

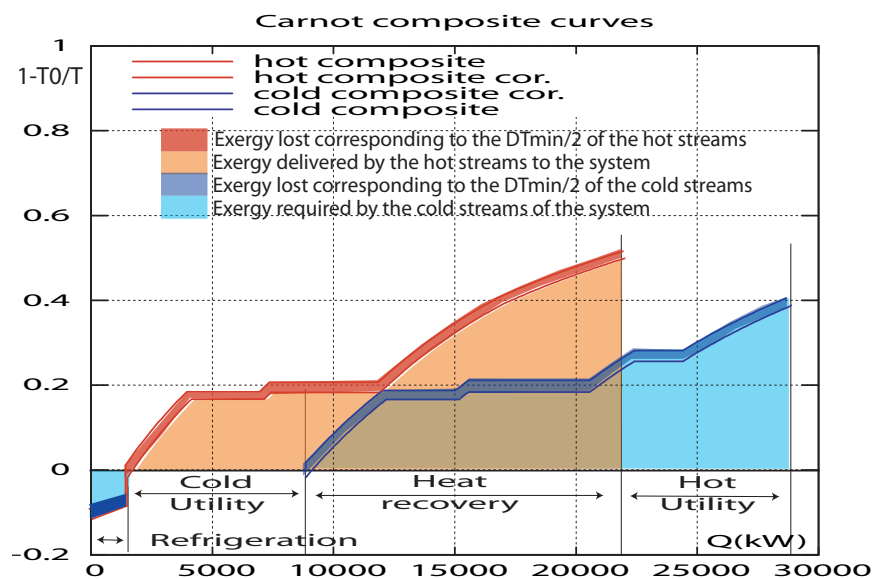
Carnot composite curves of the process

Cold composite curves



Marechal, François, and Daniel Favrat. "Combined exergy and pinch analysis for the optimal integration of energy conversion technologies." *18th International conference on efficiency, cost, optimization, simulation and environmental impact of energy systems*. 2005.

Carnot composite curves and heat recovery

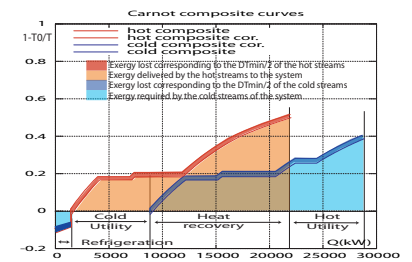


Marechal, François, and Daniel Favrat. "Combined exergy and pinch analysis for the optimal integration of energy conversion technologies." *18th International conference on efficiency, cost, optimization, simulation and environmental impact of energy systems*. 2005.

Exergy value of the heat transfer in the process

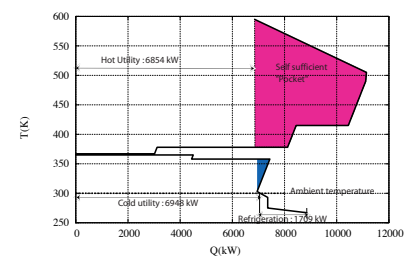
Exergy of the hot and cold process composite curves

	Energy	Exergy	Exergy	Name
		Total	$\Delta T_{min} corrected$	
Hot streams [kW]	20291.0	5521.4	5352.4	$\dot{E}q_{hot_a}$
below T_0 [kW]	1709.0	131.5	151.2	$\dot{E}q_{hot_r}$
Cold streams [kW]	20197.0	4599.3	4650.1	$\dot{E}q_{cold_a}$
below T_0 [kW]	0.0	0.0	0.0	$\dot{E}q_{cold_r}$
ΔT_{min} losses [kW]	-	-	381.2	-
Balance [kW]	1803.0	+790.0	+409.0	-



Heat recovery

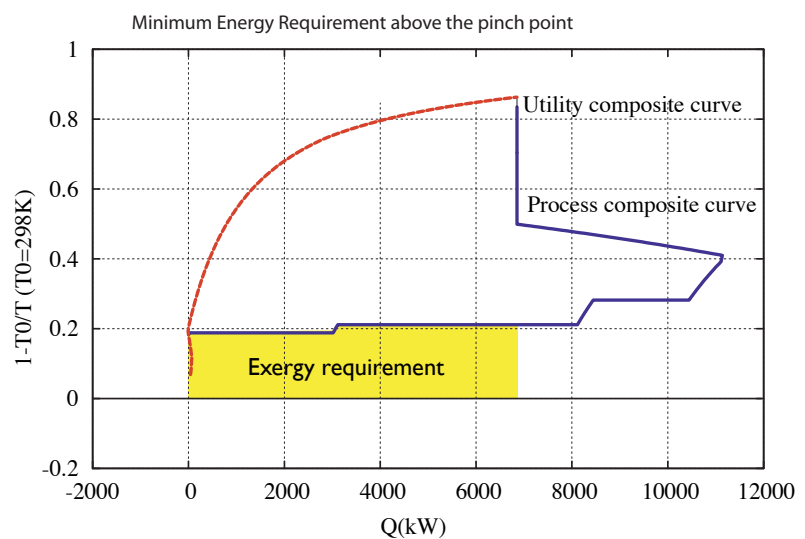
	Energy	Exergy
Heating (kW)	+6854	+567
Cooling (kW)	-6948	- 1269
Refrigeration (kW)	+1709	+ 157



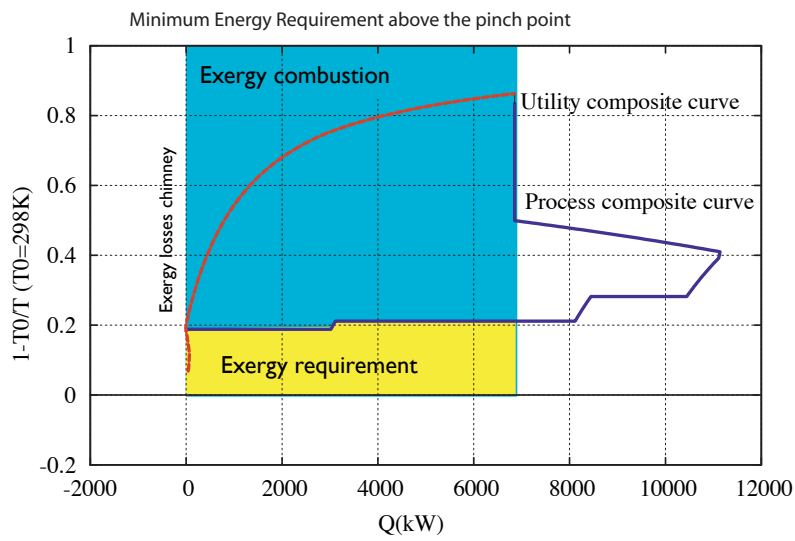
Marechal, François, and Daniel Favrat. "Combined exergy and pinch analysis for the optimal integration of energy conversion technologies." 18th International conference on efficiency, cost, optimization, simulation and environmental impact of energy systems. 2005.

Exergy requirement above the pinch

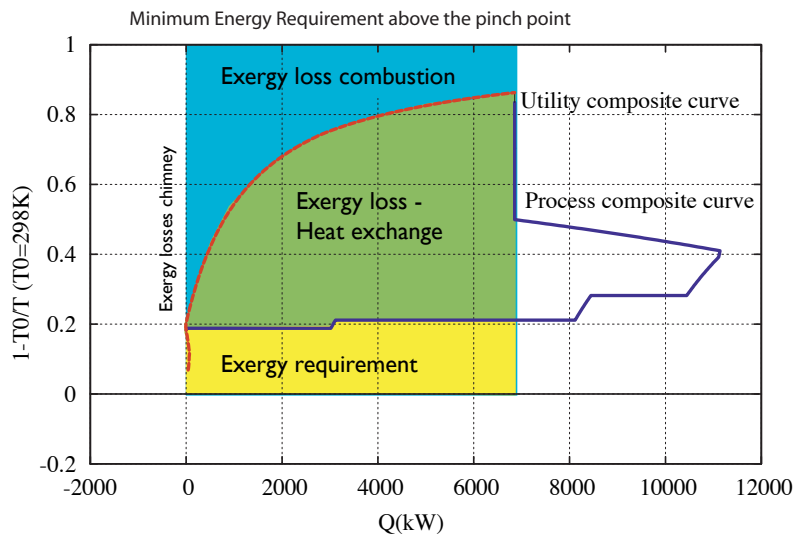
	Energy	Exergy
Heating (kW)	+6854	+567
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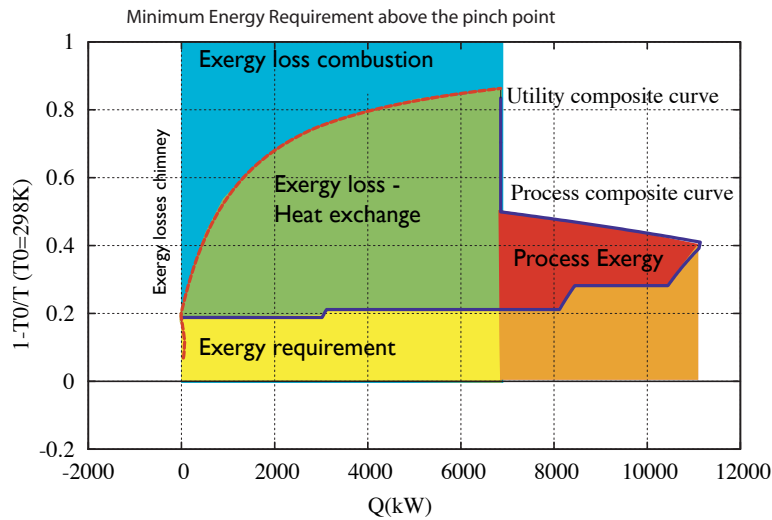
Exergy by combustion



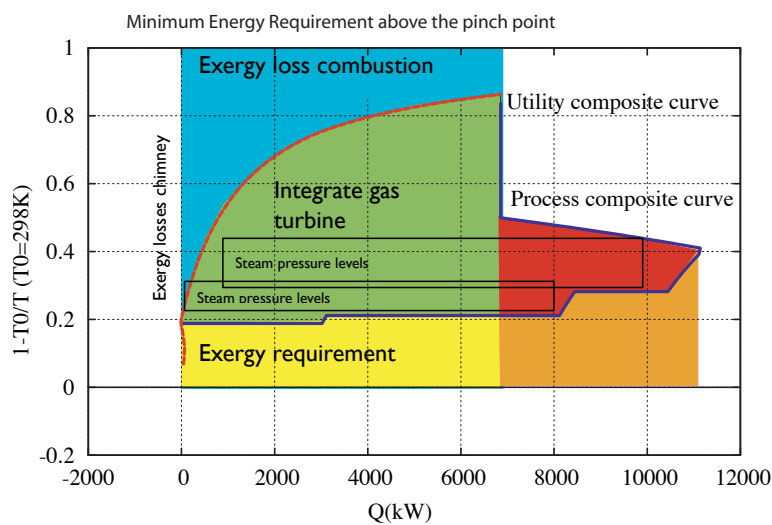
Exergy composite Heat exchange losses



Carnot composite -self-sufficient pockets

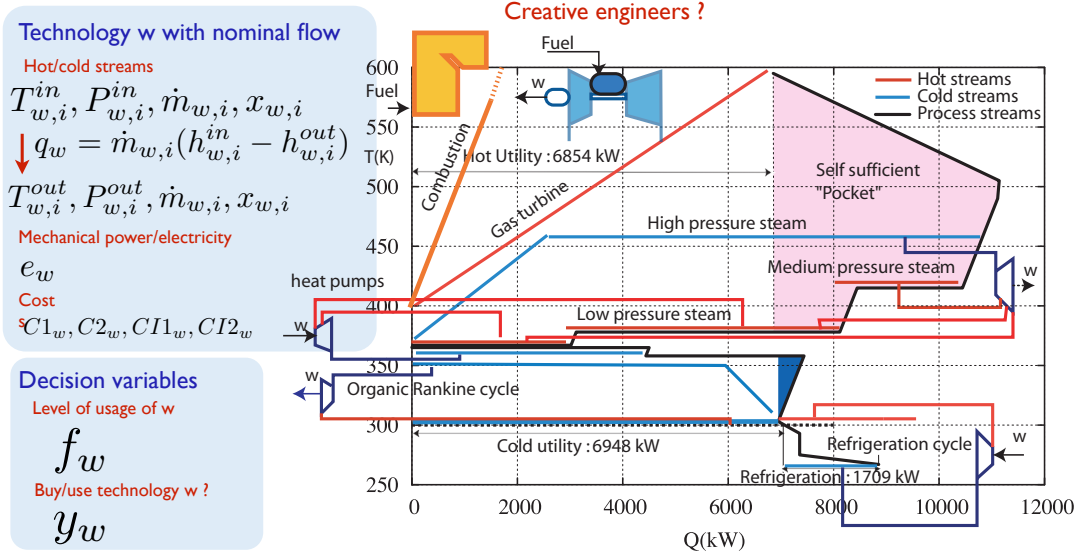


Carnot composite - suggestions to convert the exergy



What is the best way to close the energy balance with the energy resources that we buy ?

Integration of the energy conversion system



Energy conversion units with unknown flowrates

Mixed integer linear programming formulation of the process integration

$$\min_{R_r, y_w, f_w, E^+, E^-} \left(\sum_{w=1}^{n_w} C2_w f_w + C_{el} + E^+ - C_{el} - E^- \right) * t \quad \text{Operating cost}$$

$$+ \sum_{w=1}^{n_w} C1_w y_w + \sum_{w=1}^{n_w} (CI1_w y_w + CI2_w f_w) \quad \text{Investment}$$

Subject to : Heat cascade constraints

$$\sum_{w=1}^{n_w} f_w q_{w,r} + \sum_{s=1}^{n_s} Q_{s,r} + R_{r+1} - R_r = 0 \quad \forall r = 1, \dots, n_r$$

Feasibility $R_r \geq 0 \quad \forall r = 1, \dots, n_r; R_{n_r+1} = 0; R_1 = 0 \quad E^+ \geq 0; E^- \geq 0$

Electricity consumption $\sum_{w=1}^{n_w} f_w e_w + E^+ - E_c \geq 0$

Electricity production $\sum_{w=1}^{n_w} f_w e_w + E^+ - E_c - E^- = 0$

Energy conversion Technology selection $f_{min_w} y_w \leq f_w \leq f_{max_w} y_w \quad y_w \in \{0, 1\}$

Consider exergy losses

New objective function

$$\text{Min} \sum_{w=1}^{n_w} \dot{L}_w = \sum_{w=1}^{n_w} (f_w * (\sum_{f=1}^{n_{fuel,w}} \dot{m}_{f,w} \Delta k_f^0 + \dot{e}_w^+ - \sum_{r=1}^{n_r} (\dot{e}_{q_{w,r}}^- \Delta T_{min} - \dot{e}_w^-))) \quad (1)$$

– Heat exergy :

$$(\dot{e}_{q_{w,r}}^-) \Delta T_{min} = \sum_{s=1}^{n_{s,w}} \dot{q}_{s,r}^- (1 - \frac{T_0}{T_{lmr}^*})$$

where T_{lmr}^* is the logarithmic mean temperature of interval r
 $T_{lmr}^* = \frac{T_{r+1}^* - T_r^*}{\ln(\frac{T_{r+1}^*}{T_r^*})}$ when $T_{r+1}^* \neq T_r^*$ and $T_{lmr}^* = T_r^*$ otherwise

– Chemical Exergy :

$$\sum_{f=1}^{n_{fuel,w}} \dot{m}_{f,w} \Delta k_f^0$$

– Work :

$$\dot{e}_w^+ \quad \text{IN}$$

$$\dot{e}_w^- \quad \text{Out}$$

Application : the engineer creativity

Maximum energy recovery

	Energy	Exergy
Heating (kW)	+6854	+567
Cooling (kW)	-6948	- 1269
Refrigeration (kW)	+1709	+ 157

Hot utility

Boiler house : NG (44495 kJ/kg)
 Air Preheating
 Gas turbine : NG (el. eff = 32%)

Steam cycle

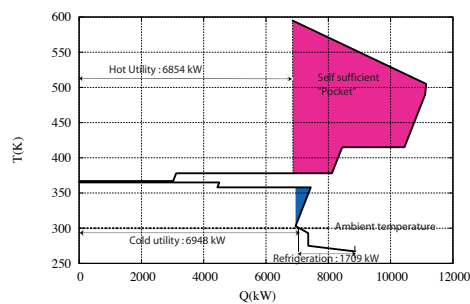
Header	P (bar)	T (K)	Comment
HP2	92	793	superheated
HP1	39	707	superheated
HPU	32	510	condensation
MPU	7.66	442	condensation
LPU	4.28	419	condensation
LPU2	2.59	402	condensation
LPU3	1.29	380	condensation
DEA	1.15	377	deaeration

Heat pumps Fluid R123

	P_{low} (bar)	T_{low} (°K)	P_{high} (bar)	T_{high} (K)	COP	kWe
Cycle 3	5	354	7.5	371	15	130
Cycle 2	6	361	10	384	12	323
Cycle 0	6	361	7.5	371	28	34

Refrigeration

Refrigerant	R717	Ammonia			
Reference flowrate	0.1	kmol/s			
Mechanical power	394	kW			
P (bar)	T_{in} (°K)	T_{out} (°K)	Q (kW)	$\Delta T_{min}/2$ (°K)	
Hot str.	12	340	304	2274	2
Cold str.	3	264	264	1880	2



Results of MILP optimisation

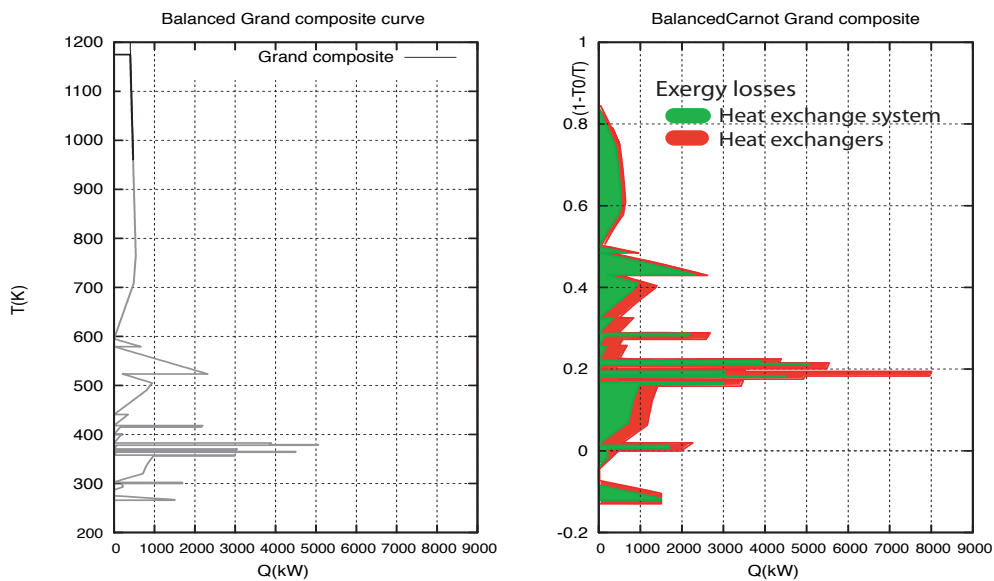
Generating multiple options

Opt	Fuel kW_{LHV}	GT kWe	CHP kWe	Cooling kW	HP kWe	
1	7071	-	-	8979	-	Comb. + frg
2	10086	-	2957	9006	-	Comb. + stm + frg
3	16961	5427	2262	9160	-	GT + stm + frg
4	-	-	-	2800	485	hpmp + frg
5	666	-	738	2713	496	hpmp + stm + frg

Share between heat pumps

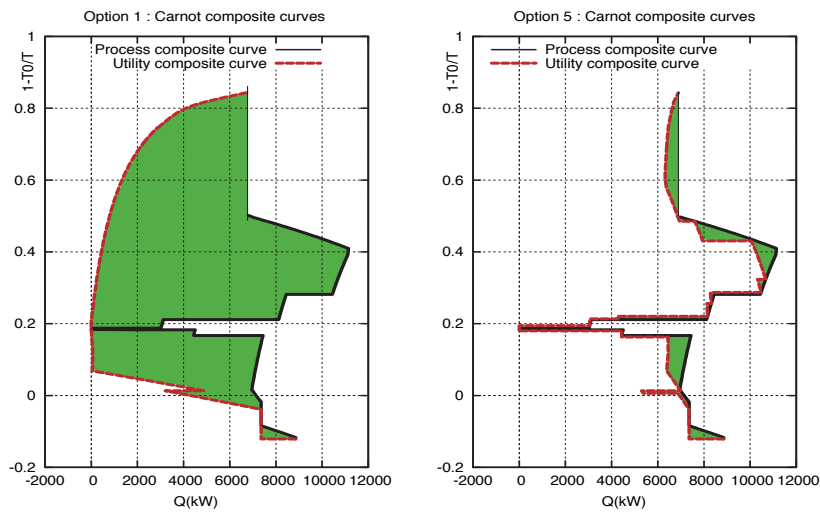
HP1 : 34 kWe
HP2 : 323 kWe
HP3 : 129 kWe

Balanced composite curves (option 5)

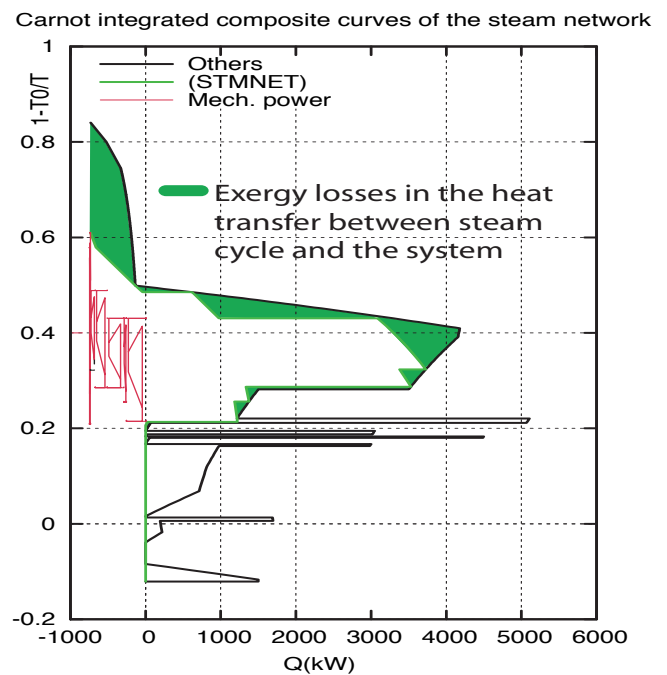
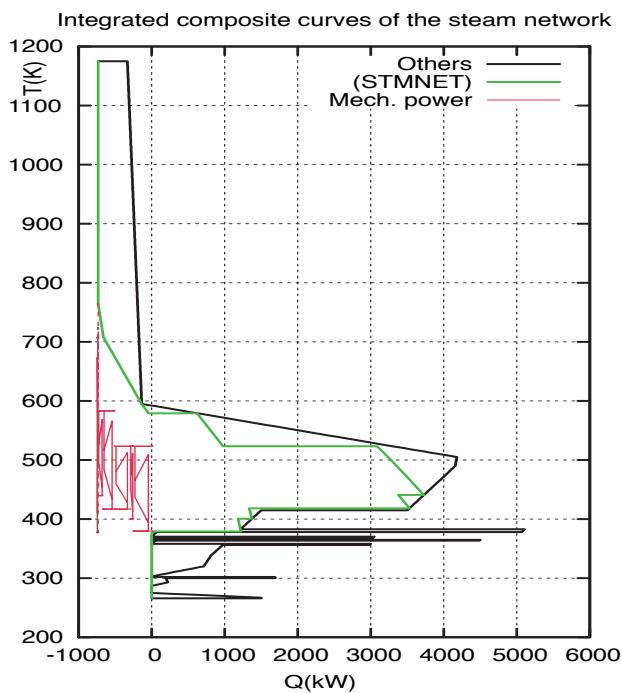


Visualising the results : Carnot composite

Tricks for creative engineers : reduce the green area !



Carnot integrated composite curves



Key performance indicator of the system

Energy efficiency

-NGCC equivalence of electricity

$$Total1 = \dot{m}_{fuel} * LHV_{fuel} + \frac{(E^+ - E^-)}{\eta_{el}} (= 55\%(NGCC))$$

-EU mix for electricity

$$Total2 = \dot{m}_{fuel} * LHV_{fuel} + \frac{(E^+ - E^-)}{\eta_{el}} (= 38\%(EU mix))$$

Exergy efficiency of the energy conversion

$$\eta_{ex} = \frac{\dot{E}q_{cold_a} + \dot{E}q_{hot_r} + \dot{E}_{grid}^-}{\dot{E}^+ + \dot{E}q_{cold_r} + \dot{E}q_{hot_a}} \quad \text{with} \quad \dot{E}^+ = \sum_{fuel=1}^{n_{fuels}} \dot{M}_{fuel}^+ \Delta k_{fuel}^0 + \dot{E}_{grid}^+$$

$$\dot{L} = (1 - \eta_{ex})(\dot{E}^+ + \dot{E}q_{cold_r} + \dot{E}q_{hot_a})$$

! Process units are sources of exergy (supply and requirements) like the energy conversion system

Results

$$Total1 = \dot{m}_{fuel} * LHV_{fuel} + \frac{(E^+ - E^-)}{\eta_{el}} (= 55\%(NGCC))$$

$$Total2 = \dot{m}_{fuel} * LHV_{fuel} + \frac{(E^+ - E^-)}{\eta_{el}} (= 38\%(EU mix))$$

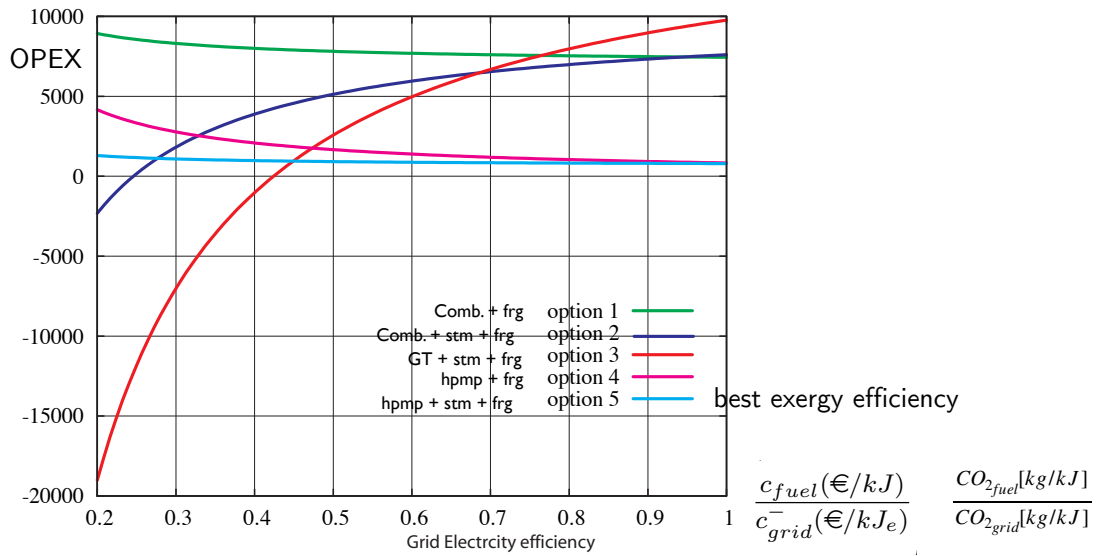
Table 9

Energy consumption and exergy efficiency of the different options

Option	Fuel [kW _{LHV}]	\dot{E}_{grid}^+ [kWe]	Total 1 [kW _{LHV}]	Total 2 [kW _{LHV}]	η_{ex} %	Losses [kW]
Comb. + frg	7071.0	371.0	7745.5	8029.7	34.9	8868.0
Comb. + stm + frg	10086.0	-2481.0	5575.1	3675.1	44.5	8830.0
GT + stm + frg	16961.0	-7195.0	3879.2	-1630.7	51.3	11197.2
hpmp + frg	0.0	832.0	1512.7	2149.9	72.4	2408.1
hpmp + stm + frg	666.0	125.0	893.3	989.0	72.6	1831.6

Exergy vs Energy cost

Exergy and costs are not always compatible



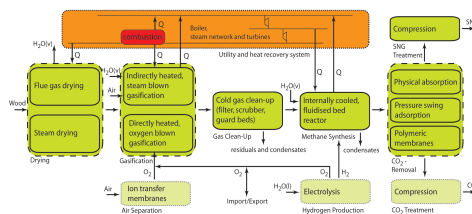
Exergy and CO2 emissions are not always compatible

Process design methodology

Super-Structure

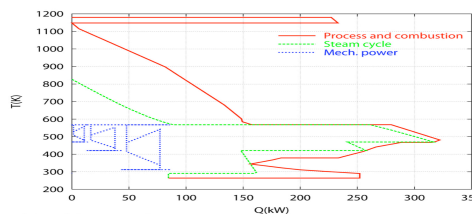
- Flowsheeting models
- Process unit operation
- Process unit options
- Exchange interfaces

Integrating heat recovery technologies in the superstructure



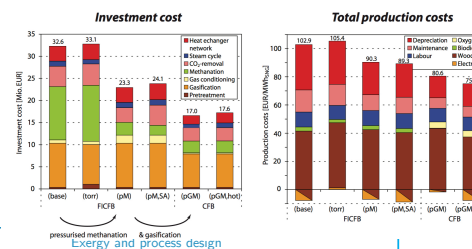
Process integration

- Energy conversion
- Heat recovery
- Energy balance

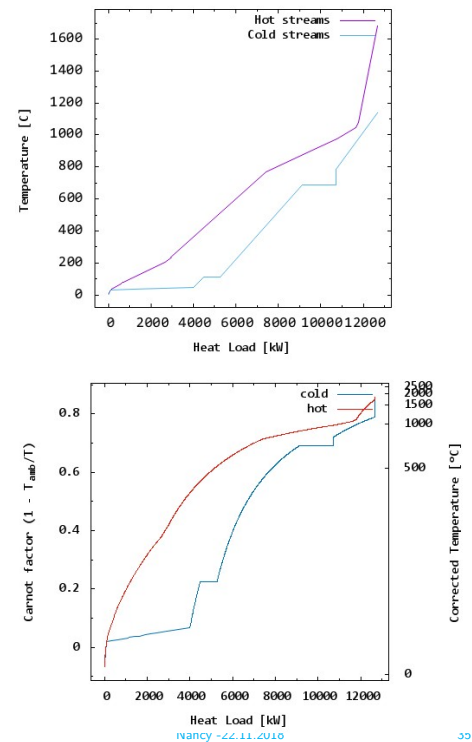
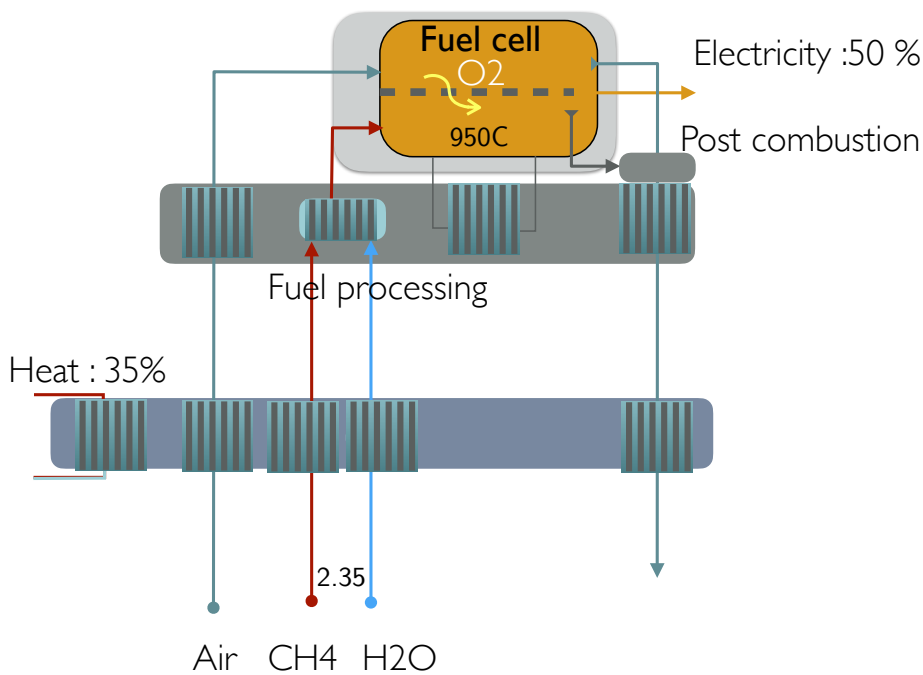


Performances

- OPEX
- CAPEX
- LCA
- Thermodynamic



Producing electricity with Fuel Cell System

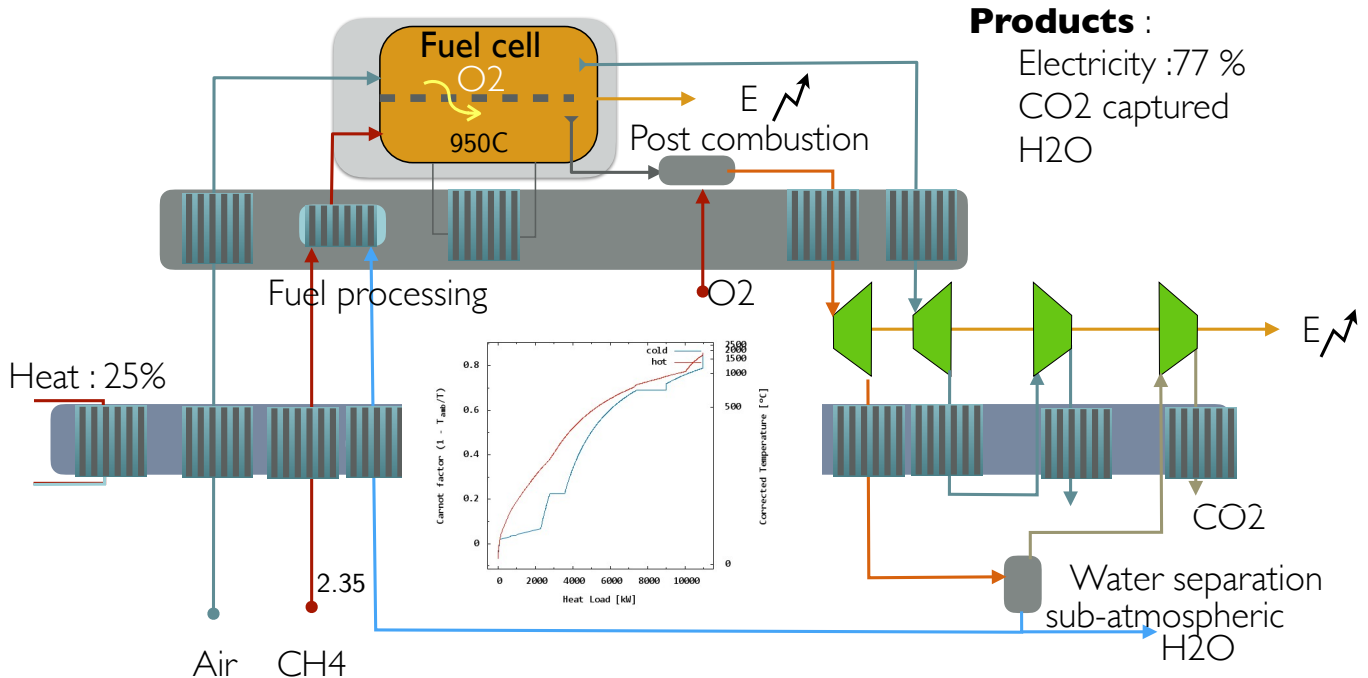


François Marechal

Exergy and process design

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Producing electricity with Fuel Cell System



Facchinetti, M, Daniel Favrat, and Francois Marechal. "Sub-atmospheric Hybrid Cycle SOFC-Gas Turbine with CO₂ Separation." *PCT/IB2010/052558*, 2011.

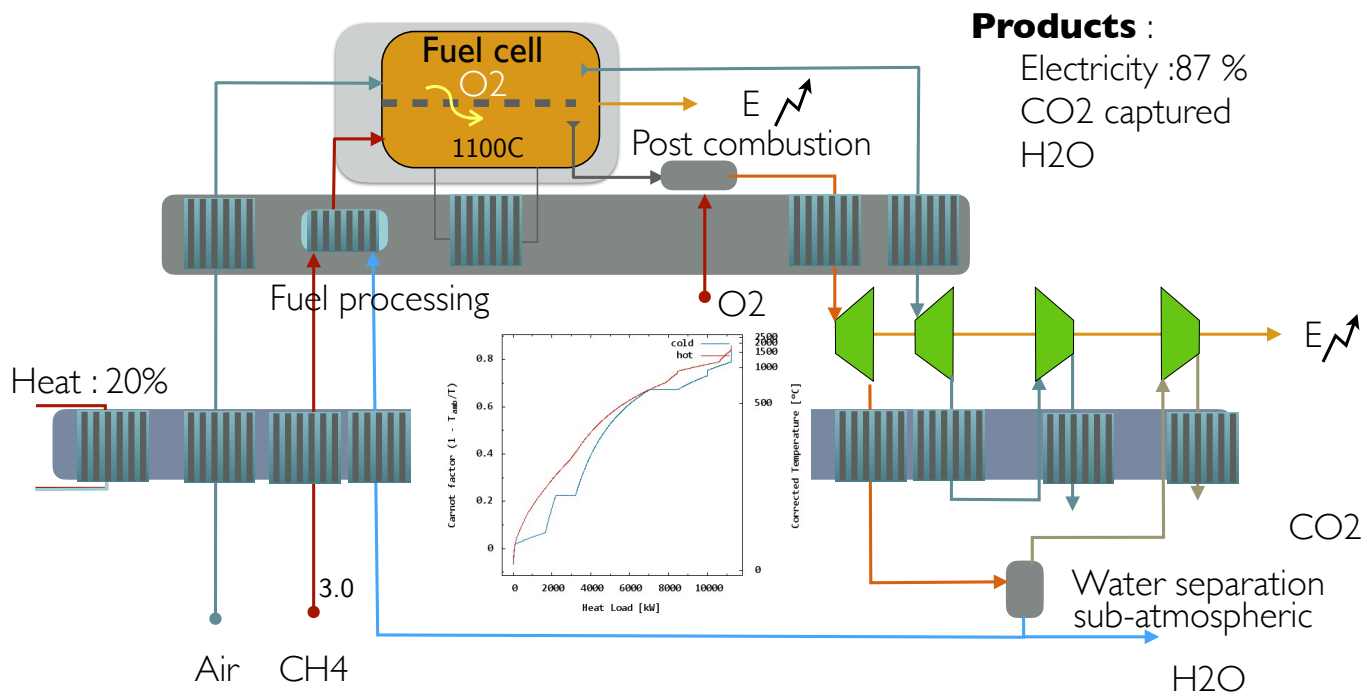
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Exergy and process design

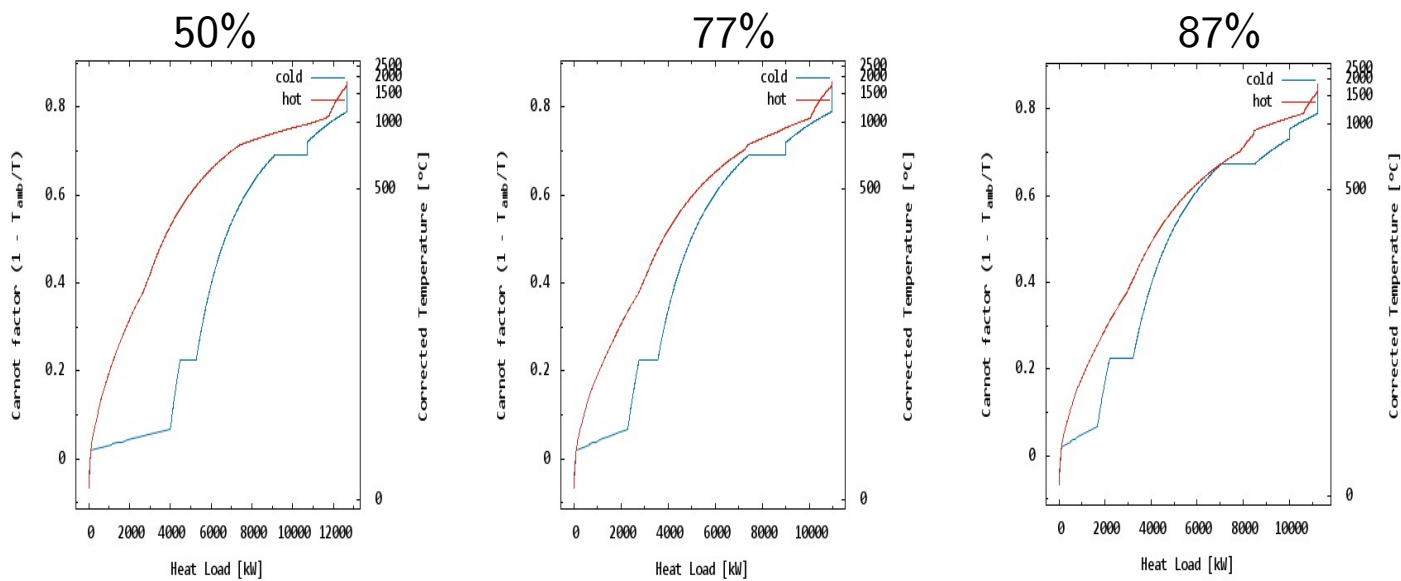
Nancy -22.11.2018

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Producing electricity with Fuel Cell System : optimised system

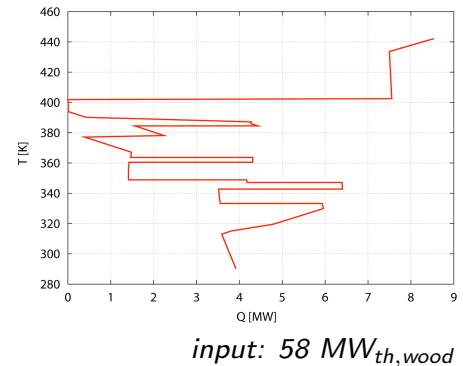
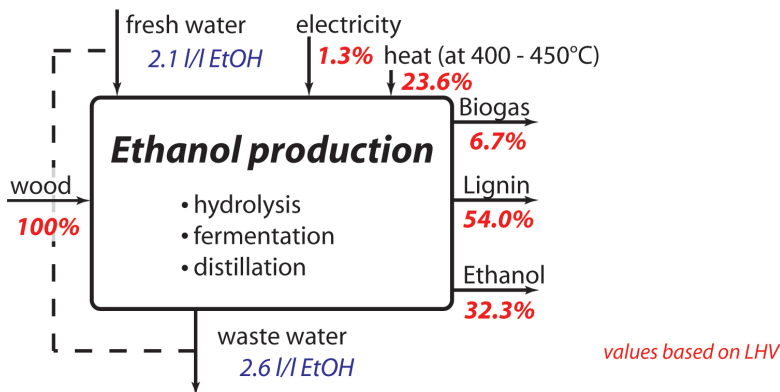


Fuel cell : SOFC-GT



Bio-refineries : system integration

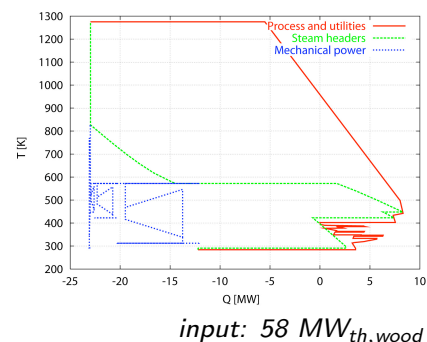
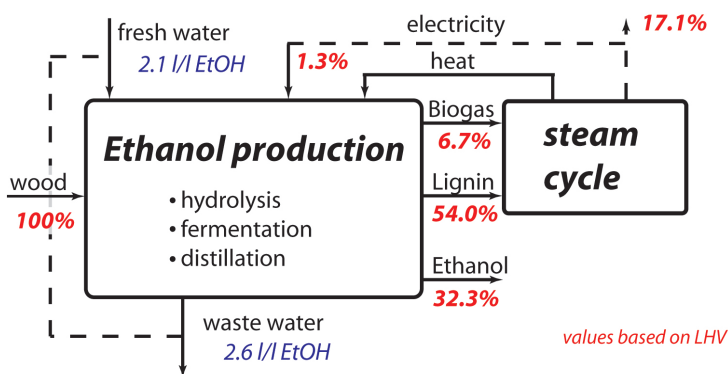
Ethanol production from lignocellulosic biomass:



Gassner, Martin, and Francois Marechal. "Increasing efficiency of fuel ethanol production from lignocellulosic biomass by process integration." *Energy & Fuels* 27.4 (2013): 2107-2115.

Converting waste streams to satisfy the process needs : CHP

Ethanol production from lignocellulosic biomass:

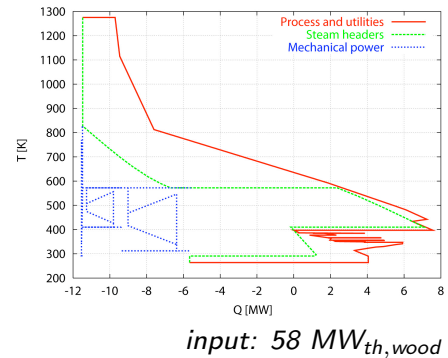
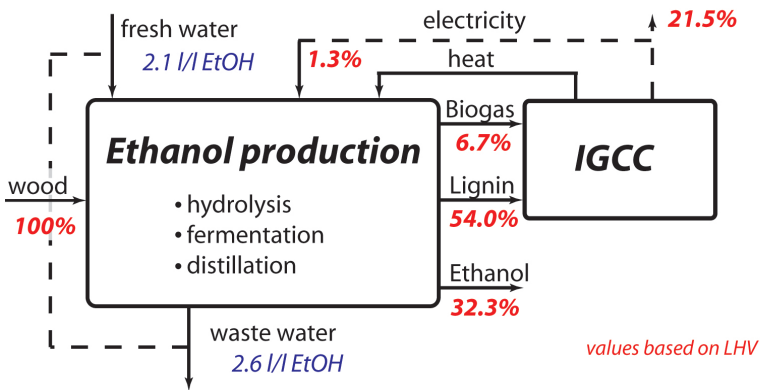


	ethanol production	steam cycle
Input	wood	100 %
	ethanol	32.3 %
Output	SNG	-
	electricity	17.1 %
chem. efficiency ($\Delta\eta_{NGCC}=55\%$)		62.3 %
total efficiency		49.4 %

Energy balance for different process integration options (without seed train, non-optimised).

Optimised CHP + power

Ethanol production from lignocellulosic biomass:

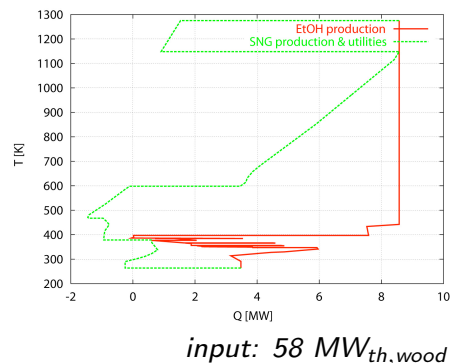
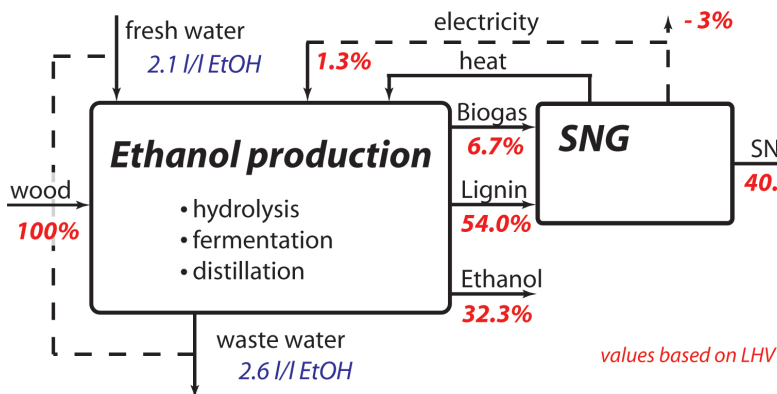


		steam cycle	IGCC
Input	wood	100 %	100 %
	ethanol	32.3 %	32.3 %
Output	SNG	-	-
	electricity	17.1 %	21.5 %
chem. efficiency ($\Delta\eta_{NGCC}=55\%$)		62.3 %	70.0 %
total efficiency		49.4 %	53.8 %



Combined heat and fuel

Ethanol production from lignocellulosic biomass:

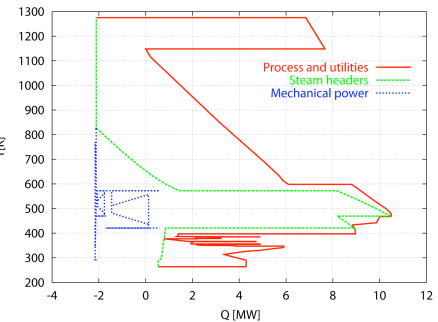
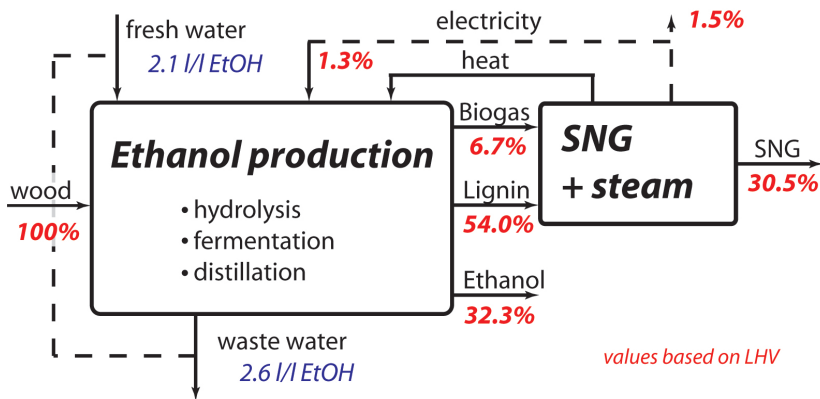


		steam cycle	IGCC	SNG
Input	wood	100 %	100 %	100 %
	ethanol	32.3 %	32.3 %	32.3 %
Output	SNG	-	-	40.3 %
	electricity	17.1 %	21.5 %	-3.0 %
chem. efficiency ($\Delta\eta_{NGCC}=55\%$)		62.3 %	70.0 %	67.3 %
total efficiency		49.4 %	53.8 %	70.5 %



combined heat - fuel and power ?

Ethanol production from lignocellulosic biomass:



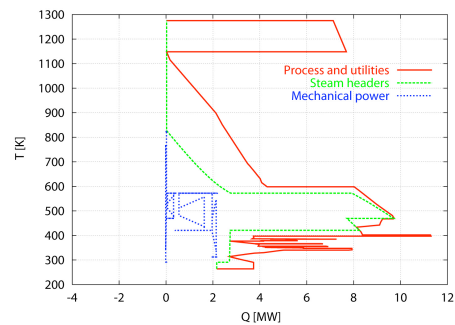
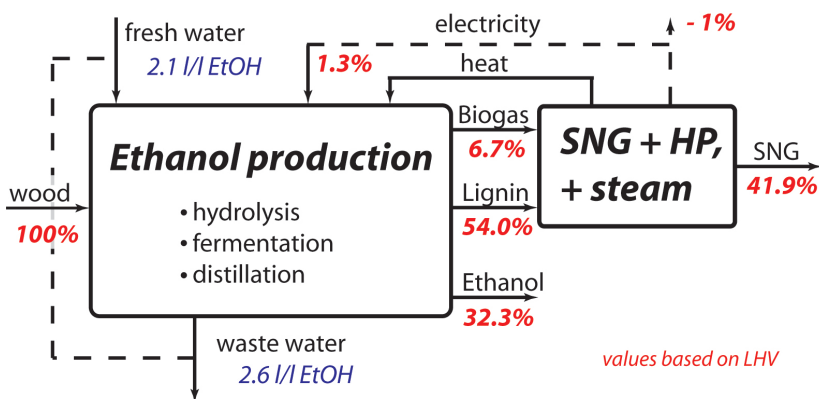
input: $58 \text{ MW}_{th,wood}$

		steam cycle	IGCC	SNG	+ steam
Input	wood	100 %	100 %	100 %	100 %
	ethanol	32.3 %	32.3 %	32.3 %	32.2 %
Output	SNG	-	-	40.3 %	30.5 %
	electricity	17.1 %	21.5 %	-3.0 %	1.5 %
	chem. efficiency ($\Delta\eta_{NGCC}=55\%$)	62.3 %	70.0 %	67.3 %	65.3 %
	total efficiency	49.4 %	53.8 %	70.5 %	64.2 %



From the exergy analysis

Ethanol production from lignocellulosic biomass:



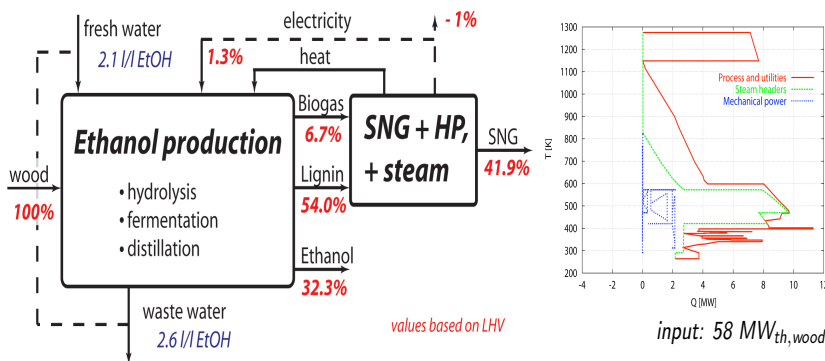
input: $58 \text{ MW}_{th,wood}$

		steam cycle	IGCC	SNG	+ steam	+ HP
Input	wood	100 %	100 %	100 %	100 %	100 %
	ethanol	32.3 %	32.3 %	32.3 %	32.2 %	32.2 %
Output	SNG	-	-	40.3 %	30.5 %	41.9 %
	electricity	17.1 %	21.5 %	-3.0 %	1.5 %	-1.0 %
	chem. efficiency ($\Delta\eta_{NGCC}=55\%$)	62.3 %	70.0 %	67.3 %	65.3 %	72.3 %
	total efficiency	49.4 %	53.8 %	70.5 %	64.2 %	73.1 %



From the exergy analysis

Ethanol production from lignocellulosic biomass:



Energy balance still holds
Extracting exergy means
extracting energy

	steam cycle	IGCC	SNG	+ steam	+ HP
Input wood	100 %	100 %	100 %	100 %	100 %
Output ethanol	32.3 %	32.3 %	32.3 %	32.2 %	32.2 %
Output SNG	-	-	40.3 %	30.5 %	41.9 %
Output electricity	17.1 %	21.5 %	-3.0 %	1.5 %	-1.0 %
chem. efficiency ($\Delta\eta_{IGCC}=55\%$)	62.3 %	70.0 %	67.3 %	65.3 %	72.3 %
total efficiency	49.4 %	53.8 %	70.5 %	64.2 %	73.1 %



Gassner, Martin, and Francois Marechal. "Increasing efficiency of fuel ethanol production from lignocellulosic biomass by process integration." *Energy & Fuels* 27.4 (2013): 2107-2115.

Conclusion : process design and exergy

Modeling and Optimisation techniques to design processes

- Flowsheet models
- Operating conditions
- Process integration
 - unit selection and interactions
- Exergy loss : (one of the) objective function

Exergy analysis

- Definition of process unit interfaces
- Carnot composite for the efficiency of the energy conversion
- Identify missing conversion units
- Reducing losses means changing flows

Any Question ?